

8. a) $2 = 1 + 1$

1 radian is about 60° .

$60^\circ + 60^\circ = 120^\circ$

2 radians is about 120° .

Therefore 2 radians is greater than 100° .

b) 0.5 is one half of 1.

1 radian is about 60° .

One half of 60° is 30° .

0.5 radians is about 30° .

Therefore 45° is greater than 0.5 radians.

c) $5 = (5)(1)$

1 radian is about 60° .

$(5)(60^\circ) = 300^\circ$

5 radians is about 300° .

Therefore 5 radians is greater than 280° .

d) $6.5 = (6)(1) + 0.5$

1 radian is about 60° .

0.5 radians is about 30° .

$(6)(60^\circ) + 30^\circ = 390^\circ$

6.5 radians is about 390° .

Therefore 400° is greater than 6.5 radians.

9. Disagree, e.g., the measure of an angle independent of the circle radius. The central angle, measured in radians, in a circle with a radius of 5 m will be the same as an equivalent angle in a circle with a radius of 10 m. For example, 180° is equal to π radians for a circle of any radius.

10. e.g., Use benchmarks to estimate the radian measure equivalent of angles greater than 360° , where 1 radian is about 60° , 3.2 radians is about 180° and 6.3 radians is about 360° . For example, determine the radian measure of

i) 480° ii) 525° iii) 650°

i) $480^\circ = 8 \cdot 60^\circ$, and $8 \cdot 1 = 8$

OR $480^\circ = 360^\circ + 90^\circ + 30^\circ$, and

$6.3 + 1.6 + 0.5 = 8.4$

ii) $525^\circ < 540^\circ$

$540^\circ = 9 \cdot 60^\circ$, and $9 \cdot 1 = 9$

OR $540^\circ = 360^\circ + 180^\circ$, and $6.3 + 3.2 = 9.5$

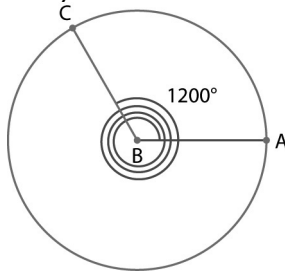
iii) $650^\circ < 660^\circ$

$660^\circ = 11 \cdot 60^\circ$, and $11 \cdot 1 = 11$

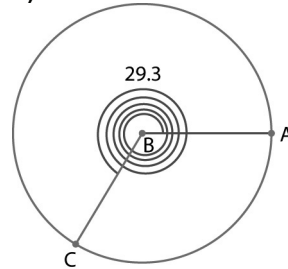
OR $660^\circ = 360^\circ + 180^\circ + 120^\circ$, and

$$2\pi + \pi + \frac{\pi}{3} = \frac{10\pi}{3}$$

11. a)



b)



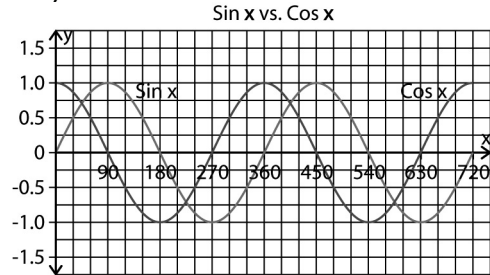
12. a) The estimate is 4.0 radians. This is because the sum of 3.2 radians (180°) and 0.8 radians (45°) is 4.0 radians or 225° . The measured angle is 227° .

b) The estimate is 3.0 radians or about 170° . This is because it looks slightly less than 3.2 radians. The measured angle is 170° .

c) This estimate is 5.9 radians because the section of the circle that is not measured looks to be approximately a sixteenth of the circle. 6.3 divided by 16 is about 0.4. 6.3 subtracted by 0.4 is 5.9 radians. This is approximately 337° in degree. The measured angle is 342° .

Lesson 8.2: Exploring Graphs of Periodic Functions, page 524

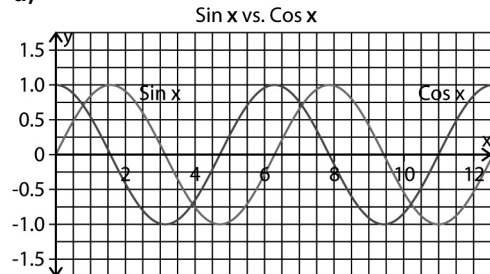
1. a)



b) When the value of $\sin x$ is a maximum, $\cos x$ is at zero. When the value of $\cos x$ is a minimum, x is equal to 180° and 540° .

c) When the value of $\cos x$ is a maximum, $\sin x$ is at zero. The value of $\sin x$ is a minimum when x is equal to 270° and 630° .

d)



2. The graph of $y = \sin x$ repeats itself after it passes through 360° or 2π .

3. e.g. The graph is symmetrical along the x -axis, with the axis of symmetry being at 90° and 270° , respectively. The graph is rotationally symmetrical around the point $(180^\circ, 0)$.

4. e.g., The graph is symmetrical along the x -axis, with the axis of symmetry being at 180° and 360° , respectively. The graph is rotationally symmetrical around the point $(270^\circ, 0)$.

5. a) The y -intercept of the graph of $y = \sin x$ is 0.
b) The y -intercept of the graph of $y = \cos x$ is 1.

6. Using the graph from chapter 1,

a) The x -intercepts of the graph of $y = \sin x$ for the interval from 0° to 720° are $0^\circ, 180^\circ, 360^\circ, 540^\circ$ and 720° .

b) The x -intercepts of the graph of $y = \cos x$ for the interval from 0° to 720° are $90^\circ, 270^\circ, 450^\circ$, and 630° .

7. e.g., The up-and-down pattern in the graph of $y = \sin x$ looks like the repeating pattern of waves in a lake.

8. Yes, because each point on the sine graph corresponds to a point on the cosine graph with the same y -coordinate but with an x -coordinate of 90° less. For example, consider the x -intercepts for $y = \cos x$ and $y = \sin x$ on 0° to 720° :

$y = \cos x$	$y = \sin x$	$y = \cos x$ translated left by 90°
90°	0°	0°
270°	180°	180°
450°	360°	360°
630°	540°	540°
...	720°	720°

The same results occur for any value of $y = \cos x$.

9. e.g., It would look like the graph of $\cos x$, as it would start at 1, decrease to 0 after spinning 90° , then decrease to -1 after spinning 180° , and so on.

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A. Looking for more precise values is a way to test the capabilities of newer computers. It is an interesting intellectual exercise. The digits in the decimal value of π occur in a random order, so it is a good random-number generator and it is useful for breaking codes.

B. i) The total surface area is $8.273\dots \text{ km}^2$.

ii) Using 3.2 as the value of π , the total surface area would have been $8.427\dots \text{ km}^2$. There would be $0.153\dots \text{ km}^2$ of wasted steel.

Lesson 8.3: The Graphs of Sinusoidal Functions, page 536

1. a) Amplitude = $\frac{\text{max} - \text{min}}{2}$

$$\text{Amplitude} = \frac{3.5 - (-3.5)}{2}$$

$$\text{Amplitude} = \frac{7}{2}$$

$$\text{Amplitude} = 3.5$$

The amplitude of the graph is 3.5 cm, and its range is $\{y \mid -3.5 \leq y \leq 3.5, y \in \mathbb{R}\}$.

b) Amplitude = $\frac{\text{max} - \text{min}}{2}$

$$\text{Amplitude} = \frac{1 - (-3)}{2}$$

$$\text{Amplitude} = \frac{4}{2}$$

$$\text{Amplitude} = 2$$

The amplitude of the graph is 2 cm, and its range is $\{y \mid -3 \leq y \leq 1, y \in \mathbb{R}\}$.

2. a) Equation of the midline:

$$y = \frac{\text{max} + \text{min}}{2} \quad \text{Amplitude} = \frac{\text{max} - \text{min}}{2}$$

$$y = \frac{3.5 + 0.5}{2} \quad \text{Amplitude} = \frac{3.5 - 0.5}{2}$$

$$y = \frac{4}{2} \quad \text{Amplitude} = \frac{3}{2}$$

$$y = 2 \quad \text{Amplitude} = 1.5$$

The equation of the midline of this graph is $y = 2$ cm, and its amplitude is 1.5 cm.

b) Equation of the midline:

$$y = \frac{\text{max} + \text{min}}{2} \quad \text{Amplitude} = \frac{\text{max} - \text{min}}{2}$$

$$y = \frac{3 + (-5)}{2} \quad \text{Amplitude} = \frac{3 - (-5)}{2}$$

$$y = \frac{-2}{2} \quad \text{Amplitude} = \frac{8}{2}$$

$$y = -1 \quad \text{Amplitude} = 4$$

The equation of the midline of this graph is $y = -1$ cm, and its amplitude is 4 cm.

3. a) Period = second max – first max

$$\text{Period} = 120^\circ - 0^\circ$$

$$\text{Period} = 120^\circ$$

The period of this graph is 120° .

b) Period = second max – first max

$$\text{Period} = 3.75 - 0.75$$

$$\text{Period} = 3$$

The period of this graph is 3.