

To earn the least amount of interest, 5 ones must be rolled. To earn the most amount of interest, 4 sixes and 1 five must be rolled.

ii) Loan - Regular Payments:

Most:

Principal Borrowed: \$12 000 (6)

Payment Frequency: Annual (1)

Interest Rate: 6% (6)

Compounding Frequency: Daily (6)

Term: 6 years (6)

Interest Charged: \$2726.46

Least:

Principal Borrowed: \$2000 (1)

Payment Frequency: Weekly (5)

Interest Rate: 1% (1)

Compounding Frequency: Annual (1)

Term: 1 year (1)

Interest Charged: \$10.16

The player would pay the least amount of interest if the player rolls 4 ones and 1 five. The player would pay the most amount of interest if the player rolls 4 sixes and 1 one.

F. When an investment is made, the player wants to try and earn the highest amount of interest possible. When a loan is taken, the player wants to pay the lowest amount of interest possible.

Lesson 2.2: Exploring Credit Card Use, page 100

1. a) Dealership credit card:

The present value is $(5000 - 5000(0.024))$, or \$4880.

The regular payment amount is \$200.

The payment frequency is 12 times a year.

The number of payments is unknown.

The payments are made at the end of the payment periods.

The annual interest rate is 15.8%.

The compounding frequency is 365 times a year.

The future value is \$0.

Using the financial application on a graphing calculator, the number of payments is 29.669... or 30.

In total, Mia will end up paying \$5933.804... or \$5933.81.

Bank loan:

The present value is \$5000.

The regular payment amount is \$200.

The payment frequency is 12 times a year.

The number of payments is unknown.

The payments are made at the end of the payment periods.

The annual interest rate is 9.8%.

The compounding frequency is 12 times a year.

The future value is \$0.

Using the financial application on a graphing calculator, the number of payments is 28.077... or 29.

In total, Mia will end up paying \$5615.429..., or \$5615.43.

b) Dealership credit card:

$$I = A - P$$

$$I = 5933.804... - 4880$$

$$I = \$1053.804...$$

Mia will pay \$1053.81 in interest using the dealership credit card.

Bank loan:

$$I = A - P$$

$$I = 5615.429... - 5000$$

$$I = \$615.429...$$

Mia will pay \$615.43 in interest on the bank loan.

c) Dealership credit card:

$$\text{Term} = 30 \cdot \frac{365}{12}$$

$$\text{Term} = 912.5$$

It will take Mia 912.5 days, or 2 years 6 months, to pay off the credit card

Bank loan:

Term = 29 months

It will take Mia 29 months, or 2 years 5 months, to pay off the bank loan

d) e.g., She should use the bank loan, because she will pay it off sooner and pay less overall.

2. Card Blue: Cash back = $2150.66 \cdot 0.03 = \$64.52$

The present value is \$2150.66.

The regular payment amount is \$200.

The payment frequency is 12 times a year.

The number of payments is unknown.

The payments are made at the end of the payment periods.

The annual interest rate is 18.5%.

The compounding frequency is 365 times a year.

The future value is \$0.

Using the financial application on a graphing calculator, the number of payments is 11.856..., or 12. The total amount of interest paid is \$220.724..., or \$220.73. Therefore, the total additional cost of using card Blue is $\$220.73 - \64.52 , or \$156.21.

Card Red: The present value is \$2150.66.

The regular payment amount is \$200.

The payment frequency is 12 times a year.

The number of payments is unknown.

The payments are made at the end of the payment periods.

The annual interest rate is 16.25%.

The compounding frequency is 365 times a year.

The future value is \$0.

Using the financial application on a graphing calculator, the number of payments is 11.707..., or 12. The total amount of interest paid is \$190.751..., or \$190.76.

Hannah should use card Blue, because the payments are for the same amount and are at the same time for both cards, but she will pay \$34.55 less using Card Blue.

3. Assume that payments begin on July 1st, and that neither card carries a balance at this point.
 Annie's credit card:
 Months 1–6:
 The present value is $3678 + 785$, or $\$4463$.
 The regular payment amount is $\$400$.
 The payment frequency is 12 times a year.
 The number of payments is 6.
 The payments are made at the end of the payment periods.
 The annual interest rate is 15.5%.
 The compounding frequency is 365 times a year.
The future value is unknown.
 Using the financial application on a graphing calculator, the future value is $\$2343.208\dots$.
 After 6 months, the balance on the credit card is $\$2343.208\dots$, or $\$2343.21$.
 Annie has paid $\$2400$.

Month 7 onward:
 The present value is $2343.21 + 75$, or $\$2418.21$.
 The regular payment amount is $\$400$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 15.5%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.
 Using the financial application on a graphing calculator, the number of payments is $6.337\dots$, or 7.
 Annie has paid $6.337\dots \cdot \$400$, or $\$2534.85$.

The total number of payments needed is 13, and the total amount paid is $\$2400 + \2534.85 , or $\$4934.85$.

Peter's credit card:
 The present value is $3678 + 785$, or $\$4463$.
 The regular payment amount is $\$400$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 18.7%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.
 Using the financial application on a graphing calculator, the total number of payments is $12.362\dots$, or 13. The total amount paid is $12.362\dots \cdot \$400$, or $\$4944.992\dots$, or $\$4945.00$.

They should use Annie's credit card, because it costs less overall.

4. a) Card A:
 The present value is $1186 + 25$, or $\$1211$.
 The regular payment amount is $\$125$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 8.9%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.

Using the financial application on a graphing calculator, the number of payments is $10.092\dots$, or 11. The total amount paid is $10.092\dots \cdot \$125$, or $\$1261.554\dots$, or $\$1261.56$.

Card B:
 The present value is $1186 + 50$, or $\$1236$.
 The regular payment amount is $\$125$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 14.9%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.
 Using the financial application on a graphing calculator, the number of payments is $10.619\dots$, or 11. The total amount paid is $10.619\dots \cdot \$125$, or $\$1327.487\dots$, or $\$1327.49$.

Shannon would pay $\$1261.60$ with card A, and $\$1327.49$ with card B.

b) i) Card B with immediate rebate of $\$75$:
 The present value is $1186 - 75 + 50$, or $\$1161$.
 The regular payment amount is $\$125$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 14.9%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.
 Using the financial application on a graphing calculator, the number of payments is $9.934\dots$, or 10. The total amount paid is $9.934\dots \cdot \$125$, or $\$1241.751\dots$, or $\$1241.76$.
 This incentive would make card B more attractive, because it now costs less to use card B than card A.

ii) 1% of $\$1186 = \11.86
 Total cost of card B = $1327.49 - 11.86$
 Total cost of card B = $\$1315.63$
 Card A is still the better choice, because it costs less than $\$1315.63$.

iii) Card B with no annual fee:
 The present value is $\$1186$.
 The regular payment amount is $\$125$.
 The payment frequency is 12 times a year.
The number of payments is unknown.
 The payments are made at the end of the payment periods.
 The annual interest rate is 14.9%.
 The compounding frequency is 365 times a year.
 The future value is $\$0$.
 Using the financial application on a graphing calculator, the number of payments is $10.1619\dots$, or 11. The total amount paid is $10.1619\dots \cdot \$125$, or $\$1270.248\dots$, or $\$1270.25$.
 Card A is still the better choice, because it costs about 8 dollars less than card B with no annual fee.