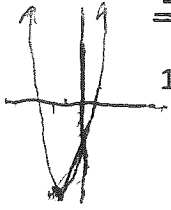


LG 5 Test B – Part B Show all your work. (Part A answers on back)



- 1) Explain as much as you can about the following quadratic equation. Include a graph if you think it will help. (vertex, domain, range, direction, intercepts, axis, min/max value)

$$y = 2(x + 2)^2 - 18$$

vertex = $(-2, -18)$

domain = $\{x \mid x \in \mathbb{R}\}$

range = $\{y \mid y \geq -18, y \in \mathbb{R}\}$

axis of symmetry: $x = -2$

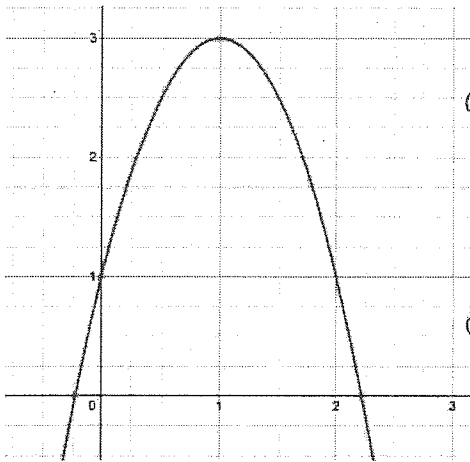
direction = opening up

y intercept = $(0, -10)$

x intercepts = $(1, 0), (-5, 0)$

minimum: $y = -18$

- 2) Using the graph below, describe as many properties of this graph of a parabola including coordinates and values that accurately describe the image.



vertex = $(1, 3)$

axis of symmetry: $x = 1$

y intercept = $(0, 1)$

x intercepts = $(-0.25, 0)$
 $(2.25, 0)$

direction: opening down

maximum: $y = 3$

domain = $\{x \mid x \in \mathbb{R}\}$

range = $\{y \mid y \leq 3, y \in \mathbb{R}\}$

(vertex)

- 3) On the coordinate grid below, sketch the graph of the following quadratic equation.

$$y = 2(x^2 - 6x + 9) + 10 - 18$$

$$y = 2x^2 - 12x + 10$$

$$y = 2(x-3)^2 - 8$$

$(3, -8)$

(y int)

$$y = 2(0^2) - 12(0) + 10$$

$$y = 10$$

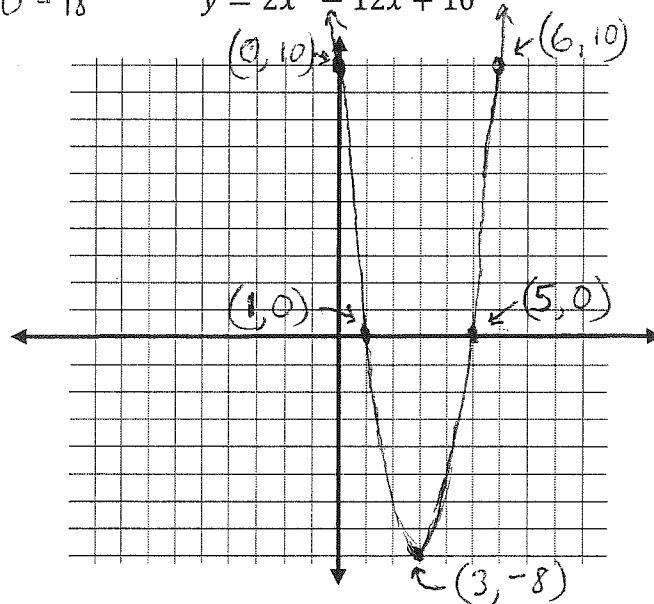
(x int)

$$0 = 2(x-3)^2 - 8$$

$$\frac{8}{2} = \frac{2}{2}(x-3)^2$$

$$4 = (x-3)^2$$

$$\pm 2 = x - 3 \quad x = 3 \pm 2$$



- 4) Use completing the square technique to convert the following equation from standard form into vertex form.

$$y = -2x^2 + 10x - 8$$

$$\left(\frac{5}{2}\right)^2 = \frac{25}{4}$$

$$y = -2(x^2 - 5x) - 8$$

$$y = -2\left(x^2 - 5x + \frac{25}{4}\right) - 8 + \frac{25}{2}$$

$$y = -2\left(x - \frac{5}{2}\right)^2 + 4\frac{1}{2}$$

- 5) The fuel consumption for a vehicle is related to the speed that it is driven. Engines are generally more efficient at higher speeds than at lower speeds. For a particular type of car driving at a constant speed, the fuel consumption, C , in litres per one hundred thousand kilometres, is related to the average driving speed, v , in kilometres per hour, by the function...

$$C = 4v^2 - 600v + 30,000$$

Determine the most efficient speed at which this car should be driven in order to keep the fuel cost at a minimum.

$$C = 4(v^2 - 150v + 5625) + 30,000 - 22,500 \quad \left(\frac{150}{2}\right)^2 = 75^2$$

$$C = 4(v - 75)^2 + 7,500$$

$$v - 75 = 0$$

$$v = 75 \frac{\text{km}}{\text{hr}}$$

Answers for page 1 - Multiple Choice

- ① C ② A ③ B ④ B ⑤ C ⑥ A ⑦ D ⑧ D