

Name: \_\_\_\_\_

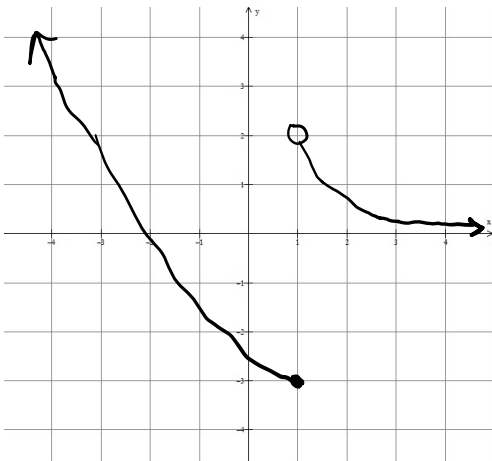
Date: \_\_\_\_\_

## Calculus 12 LG 2-3 Quiz Ver B

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1. Consider the following function  $y = f(x)$ . Find:

(1/2 mark each)



a)  $\lim_{x \rightarrow 1^-} f(x)$

b)  $\lim_{x \rightarrow 1^+} f(x)$

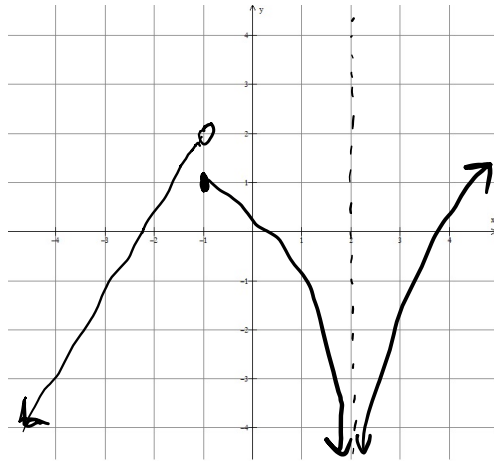
c)  $\lim_{x \rightarrow 1} f(x)$

d)  $f(1)$

e)  $\lim_{x \rightarrow -\infty} f(x)$

f)  $\lim_{x \rightarrow +\infty} f(x)$

2. For what values of  $x$  does the limit exist in the following function? (2 marks)



3. Determine the following limits. (2 marks each)

a)  $\lim_{x \rightarrow 5} \frac{2x-3}{x^2-1}$

b)  $\lim_{x \rightarrow +\infty} \frac{4x^2-7}{6x-12x^3}$

c)  $\lim_{x \rightarrow 4^+} \frac{3-x}{x^2-2x-8}$

d)  $\lim_{x \rightarrow -\infty} \frac{3-2x}{\sqrt{4x^2+1}}$

4. Determine the following limits. (2 marks each)

a)  $\lim_{x \rightarrow 0^+} \frac{\sin x}{3x}$

b)  $\lim_{x \rightarrow 0} \frac{\sin 4x}{\tan 6x}$

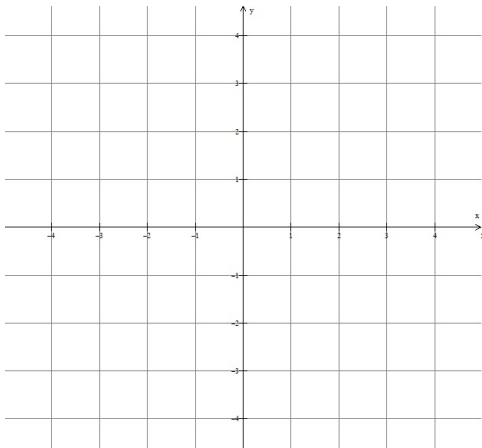
5. Find the points of discontinuity (if any). (2 marks each)

a)  $f(x) = \frac{2x-1}{x^2-x-12}$

b)  $f(x) = \begin{cases} 2x^2 - 3, & x < -2 \\ 3 - x, & x \geq -2 \end{cases}$

6. Sketch the graph of a function that is continuous everywhere but has a non-removable discontinuity at  $x=-2$  and is also not continuous at  $x=1$  but it continuous from the left.

(2 marks)



7. Prove that the function  $f(x) = \frac{3x-4}{2x^2-9x-5}$  is not continuous at  $x = 5$ . Is the discontinuity removable? (3 marks)