

Name: \_\_\_\_\_

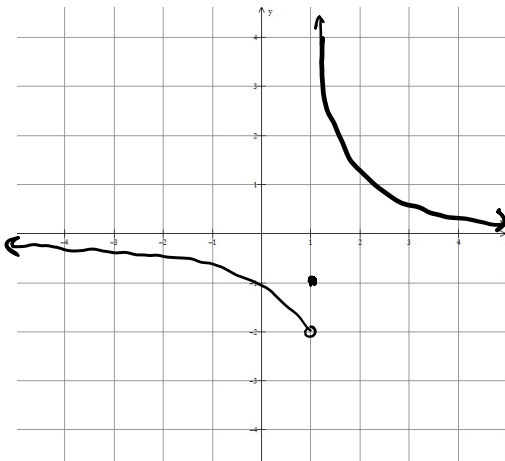
Date: \_\_\_\_\_

## Calculus 12 LG 2-3 Quiz Ver A

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1. Consider the following function  $y = f(x)$ . Find:

(1/2 mark each)



a)  $\lim_{x \rightarrow 1^-} f(x)$

b)  $\lim_{x \rightarrow 1^+} f(x)$

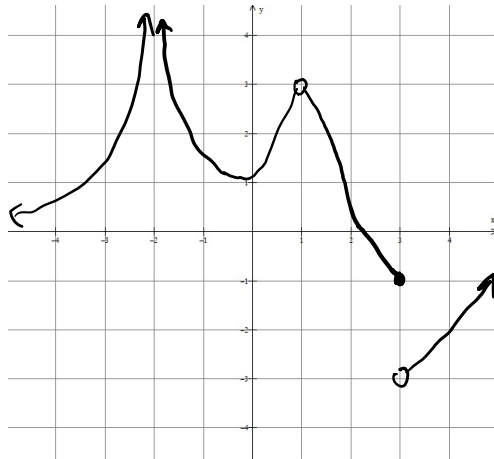
c)  $\lim_{x \rightarrow 1} f(x)$

d)  $f(1)$

e)  $\lim_{x \rightarrow -\infty} f(x)$

f)  $\lim_{x \rightarrow +\infty} f(x)$

2. For what values of  $x$  does the limit exist in the following function? (2 marks)



3. Determine the following limits. (2 marks each)

a)  $\lim_{x \rightarrow 5} \frac{x-5}{x^2-25}$

b)  $\lim_{x \rightarrow +\infty} \frac{5x-4x^3}{2x^3+4x-3}$

c)  $\lim_{x \rightarrow 2^-} \frac{x}{x^2+3x-10}$

d)  $\lim_{x \rightarrow -\infty} \frac{7x-4}{\sqrt{2+3x^2}}$

4. Determine the following limits. (2 marks each)

a)  $\lim_{x \rightarrow 0} \frac{2\sin 3x}{x}$

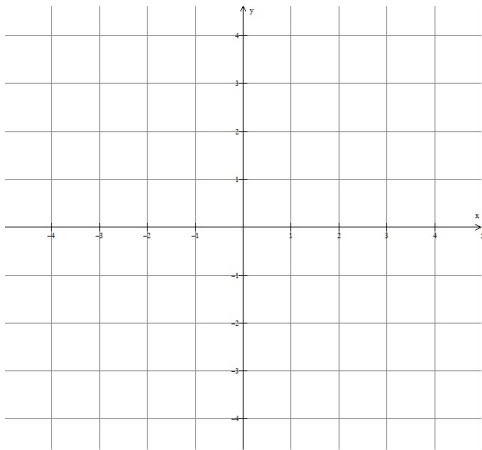
b)  $\lim_{x \rightarrow 0} \frac{\sin 2x}{\sin 6x}$

5. Find the points of discontinuity. (2 marks each)

a)  $f(x) = \frac{2}{x-3} + \frac{4}{x}$

b)  $f(x) = \begin{cases} 5x - 3, & x < 3 \\ 6 - x, & x \geq 3 \end{cases}$

6. Sketch the graph of a function that is continuous everywhere but has a removable discontinuity at  $x=-3$  and is also not continuous at  $x=2$  but it continuous from the right. (2 marks)



7. Prove that the function  $f(x) = \frac{x-2}{2x^2-3x-2}$  is not continuous at  $x = 2$ . Is the discontinuity removable? (3 marks)