

Name: \_\_\_\_\_

Date: \_\_\_\_\_

1. Find the area of the region between the curves  $y = x^2$  and  $y = x + 6$  on the interval  $[0, 2]$ . (3 marks)

2. Find the area enclosed by the curves  $x^2 = y$  and  $x = y - 2$ . (3 marks)

3. Find a horizontal line  $y = k$  that divides the area between  $y = x^2$  and  $y = 9$  into two equal parts. (3 marks)

4. The base of a certain solid is the region enclosed by  $y = \sqrt{x}$ ,  $y = 0$ , and  $x = 4$ . Every cross section perpendicular to the x-axis is a square. Determine the volume. (3 marks)

5. Find the volume of the solid that results when the region  $y = \sqrt{x}$ ,  $y = 12 - x$ , and  $x = 0$  is revolved about the x-axis. (3 marks)

6. Solve the differential equation:  $\frac{dy}{dx} = \cos 2x$

(3 marks)

7. Solve the initial value problem.  $\frac{dy}{dx} = y(1 - x^2)$ ,  $y(0) = 2$

(3 marks)

8. In the year 2000, the population of a town was 12,000 people. Since then, the population of the town has been growing by 2% per year. Let  $y = y(t)$  be the population of the town  $t$  years later.

a) Find a formula for  $y(t)$ . (2 marks)

b) When will the population of the town reach 20,000 people? (2 marks)